COMP 3270 Assignment 4 (100 points)

**Due by 11:59PM on Friday, July 29th, 2022**

Instructions:

1. Late submissions **will not** be accepted unless prior permission has been granted or there is a valid and verifiable excuse.
2. Think carefully; formulate your answers, and then write them out concisely using English, logic, mathematics and pseudocode (no programming language syntax).
3. Type your final answers in this Word document.
4. Don’t turn in handwritten answers with scribbling, cross-outs, erasures, etc. If an answer is unreadable, it will earn zero points. **Neatly and cleanly handwritten submissions are acceptable**.

**1. (15 points)** Show d and π values that result from running Breadth First Search on the directed graph below using vertex 3 as the start node.

π = NIL

d= ∞

d= 3

π = 4

d= 0

π = NIL

d= 1

π = 3

π = 5

π = 3

d= 2

d= 1

**2. (10 points)** Show how Depth First Search works on the graph below by marking on the graph the discovery and finishing times (d and f) for each vertex and the classification of each edge. Assume that the for loops in DFS and DFS-VISIT consider vertices alphabetically.

17/20

1/16

D=/F=

2/7

8/15

18/19

13/14

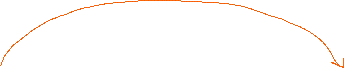
9/12

4/5

3/6

10/11

**3. (15 points)** List the vertices of the graph below in Topological Order, as produced by the Topological Sort algorithm. Assume that the for loops in DFS and DFS-VISIT consider vertices alphabetically.



p n o s m r y v x w z u q t



**4. (15 points)** Do Problem 24.1-1 (p. 654) (you do not have to do the last part, i.e., running the algorithm again after changing an edge weight).

5

X

T

-2

6

8

-3

SS

2

7

-4

7

9

Z

Y

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| Z | X | Y | T | S |
| 0 | 7 | 9 | 5 | 2 |

|  |  |  |
| --- | --- | --- |
| Note | D | Parent Id |
| Z | 0 | NIL; NIL |
| X | 1 | 0; Z |
| Y | 2 | 2; S |
| T | 2 | 7; X |
| S | 1 | 0; Z |

**5. (15 points)** Do Problem 24.2-1 (p. 657 of the recommended text). Show the results similar to Fig. 24.5.

**6.(20 points)** Do Problem 24.3-1 (p. 662 of the recommended text).

T

X

6

3

2

2

4

1

S

7

1

5

3

6

Y

Z

* Unvisited Nodes: [s⃰⃰, t, x, y, z]
* Second Pass (s):
* s = 0, t = 3, y = 5, x = ∞, z = ∞
* Unvisited: [s⃰, t⃰, x⃰, y⃰, z, ]
* Third Pass (t):
* s = 0, t = 3, y = 5, x = 9, z = ∞
* Unvisited: [s⃰, t⃰, x⃰, y⃰, z⃰, ]
* Fourth Pass (y):
* s = 0, t = 3, y = 5, x = 9, z = ∞
* Unvisited: [s⃰, t⃰, x⃰, y⃰, z⃰, ]
* Fifth Pass (z):
* s = 0, t = 3, y = 5, x = 9, z = ∞
* Unvisited: [s⃰, t⃰, x⃰, y⃰, z⃰, ]

x

t

6

D = 2

Π = t

3

s

D = 1

Π = s

D = 0

Π = NIL

5

D = 2

Π = y

6

z

y

D = 1

Π = s

t

6

x

3

4

2

7

1

2

s

3

5

6

z

y

* Unvisited Nodes: [s⃰⃰, t, x, y, z]
* First Pass (t):
* s = 3, t = ∞, x = 7, y = ∞, z = 0
* Unvisited: [s, t, x, y, z⃰, ]
* Second Pass (s):
* s = 3, t = 6, x = 7, y = 8, z = 0
* Unvisited: [s⃰, t, x, y, z⃰, ]
* Third Pass (t):
* s = 0, t = 3, y = 5, x = 9, z = ∞
* Unvisited: [s⃰, t⃰, x, y, z⃰, ]
* Fourth Pass (y):
* s = 0, t = 3, y = 5, x = 9, z = ∞
* Unvisited: [s⃰, t⃰, x, y⃰, z⃰, ]
* Fifth Pass (x):
* s = 3, t = 6, x = 7, y = 8, z = 0

x

D = 1

Π = z

D = 2

Π = s

3

2

s

7

3

D = 1

Π = z

D = 0

Π = NIL

D = 3

Π = t

y

z

**(7) (10 points)** Supposethat a graph G has a Minimum Spanning Tree (MST) computed. How quickly can we update the MST if we add a new vertex and incident edges to G. Propose and outline a strategy and present an algorithm (you can reuse graph algorithms covered in class as building blocks as part of your solution) and evaluate its asymptotic complexity.

* When a new component is added to an MST, you create a union of the two MSTs. Adding a new vertex will result in a new minimum spanning tree. Finding the shortest path to each vertex in graph G will require a greedy MST strategy.
* Sorting the edges by weight, add edges to the MST ranging from the smallest to the largest edge. It will also add edges that do not form a cycle to then achieve a proper MST for computation.
* This would run O(E logV) where E contains the incident edges that are added in this process.